Efficient frequency conversion in slab waveguide by cascaded nonreciprocal interband photonic transitions

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A slab-waveguide-based configuration for efficient frequency conversion is proposed. In the proposed structure, frequency conversion is induced through cascaded multistep nonreciprocal interband photonic transitions activated by external refractive-index modulations. The advantages of interband photonic transition over intraband photonic transition for frequency conversion are analyzed with the coupled-mode theory. © 2010 Optical Society of America

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Investigation on the analogy of photonics to electronics creates great opportunity to invent novel concepts and technological breakthroughs that can overcome the fundamental limitations of modern electronics in bandwidth, speed, and capacity. In this context, we see a strong need for investigating the inter- or intraband transition mechanism of photons in photonic structures for reaching the full potential of photonic devices.

Recently, Yu and Fan proposed a novel mechanism of complete optical isolation by nonreciprocal interband photonic transitions using time-varying structural refractive-index perturbation [1,2]. The nonreciprocal interaction of light and matter has been researched intensively owing to its fundamental importance [3–5], which provides a basic mechanism for realizing novel photonic devices, such as a photonic isolator, diode, and transistor. It was also shown that frequency conversion is enabled in a nonreciprocal linear manner using time-varying structural refractive-index perturbation. Frequency conversion can be realized by several mechanisms as nonlinear harmonic generation [5], Doppler shift in dynamically tuned microcavities [6], and so on. Interestingly, frequency conversion and linear and nonlinear nonreciprocal interactions are closely related and occur simultaneously in many cases.

In this Letter, we propose a configuration of cascaded multistep linear nonreciprocal interband transitions for efficient frequency conversion in a slab waveguide with time-varying structural refractive-index perturbation. In the proposed structure, frequency conversion is induced through interband or intraband photonic transition, and the amount of frequency change can be controlled arbitrarily. This is a distinctive point from frequency conversion by nonlinear harmonic generation. Considering that the dynamic range of single-step frequency conversion with a single photonic band transition is limited to be small, we address the multistep photonic band transition as an effective manner to attain large frequency variation.

The frequency conversion processes in a slab waveguide are divided into two ways principally: intraband photonic transition and interband photonic transition. The frequency conversion based on interband and intraband transitions can be analyzed with the coupled-mode theory. Consider a slab waveguide with a width of w and a permittivity of $\varepsilon_S$. As in [1], this slab waveguide is supposed to have a localized single modulation region, where the perturbation of permittivity is given by $\varepsilon'(r, t) = \delta(x)(qz - \Omega t)$, as shown in Fig. 1(a), which occupies one half of the slab waveguide. In practice, this kind of modulation would be realized by electrical and optical impact ionization structures [6,7], optomechanical crystals [8], and so on. In the coupled-mode theory of a single transition of $(\omega_i, \beta_i) \rightarrow (\omega_f, \beta_f)$ induced by the permittivity perturbation $\varepsilon'(r, t)$, three related optical modes are included. The y-directional electric field in the structure is represented by the coupled-mode analysis form

$$E(r, t) = a_i(z)E_i(x)e^{j(\beta_i z - \omega_i t)} + a_f(z)E_f(x)e^{j(\beta_f z - \omega_f t)} + a_n(x)e^{j(\beta_n z - \omega_n t)},$$

where $E_i(x)e^{j(\beta_i z - \omega_i t)}$, $E_f(x)e^{j(\beta_f z - \omega_f t)}$, and $E_n(x)e^{j(\beta_n z - \omega_n t)}$ are normalized eigenmodes having unit power equal to 1. $a_i(z)$, $a_f(z)$, and $a_n(z)$ indicate the optical power flux of the respective modes. The first mode is the initial mode, $E_i$ with $\omega_i$ and $\beta_i$, and the second mode is the transition mode, $E_f$ with $\omega_f = \omega_i + \Omega$ and wavenumber $\beta_f$. The phase mismatch in this transition is denoted by $\Delta\beta_i = \beta_f - \beta_i - q$. The third mode is denoted by $E_n$ with a frequency of $\omega_n = \omega_i - \Omega$ and wavenumber $\beta_n$. The phase mismatch in this interband transition is denoted by $\Delta\beta_{i,n} = \beta_n - \beta_i + q$. The wavenumbers are determined by the dispersion relation of the slab waveguide.

By substituting Eq. (1) into Maxwell’s equations, we obtain the following coupled-mode equation system under the slowly varying amplitude approximation as
\[
\begin{bmatrix}
\frac{da_i(z)}{dz} \\
\frac{da_f(z)}{dz} \\
\frac{da_n(z)}{dz}
\end{bmatrix}
= \begin{bmatrix}
0 & jC_{i,f}e^{j\Delta \beta_{i,z}} & jC_{i,n}e^{j\Delta \beta_{i,n,z}} \\
-jC_{f,i}e^{-j\Delta \beta_{i,z}} & 0 & 0 \\
-jC_{n,i}e^{-j\Delta \beta_{i,n,z}} & 0 & 0
\end{bmatrix}
\begin{bmatrix}
a_i(z) \\
a_f(z) \\
a_n(z)
\end{bmatrix},
\]

(2)

where the coupling parameters, \(C_{i,f}, C_{f,i}, C_{i,n}, \) and \(C_{n,i}\), are given, respectively, by

\[
C_{a,b} = (\varepsilon_0 \omega_0 / 8) \int_{-\infty}^{\infty} \delta(x) \times E_a(x) E_b(x) dx,
\]

for \((a, b) = (i, f), (f, i), (i, n), \) and \((n, i)\). Equation (2) can be numerically solved by the fourth-order Runge–Kutta method.

Figure 1(a) shows the simulation result of the interband transition between symmetric mode \(p_1\) and asymmetric mode \(p_2\). In the simulations, the slab waveguide thickness of \(w = 0.22 \mu m\), the permittivity of \(\varepsilon_S = 12.25\), the first-mode frequency of \(\omega_1 = 0.9\), and the second-mode frequency of \(\omega_2 = 1.15\) are used. The value of frequency is a normalized value by \(2\pi c / a\), where \(c\) and \(a\) are light speed in vacuum and 1 \(\mu m\), respectively.

The length of modulation region is set to 21.9 \(\mu m\). The coupled-mode theory shows that the optical power is exchanging between symmetric mode \(p_1\) and asymmetric mode \(p_2\) along the \(z\) axis. The modulation invokes the variation of the total optical power conveyed by the optical modes as well as mode conversion. The high-frequency mode has higher power because the photon energy is proportional to frequency. It can be understood that the energy of the carrier signal is added to or subtracted from optical mode propagating in the slab waveguide. In Fig. 1(b), the electric field profile showing the interband photonic transitions is presented. In the band diagram, this kind of transition can be graphically

Fig. 1. (Color online) (a) Interband photonic transition in a slab waveguide between symmetric mode \(p_1(\omega_1, \beta_1)\) and asymmetric mode \(p_2(\omega_2, \beta_2)\). (b) \(y\)-directional electric field distribution \(|E_y|\).

Fig. 2. (Color online) Cascaded multistep interband photonic transitions: (a) four-step interband photonic transitions \((p_1 \rightarrow p_2 \rightarrow p_3 \rightarrow p_4 \rightarrow p_5)\); (b) optical power exchange along the \(z\) axis and \(y\)-directional electric field distribution \(|E_y|\).
transitions enable mode frequency to increase or decrease stepwise. In Fig. 2(b), the electric field profile of the four-step interband transitions with the indication of modulation regions is shown, and the optical power exchange along the \( z \) axis of each mode is plotted. It is seen that the optical power is dependent on optical frequency. The input optical mode with optical frequency of \( \omega_1 \) is efficiently converted to the final optical mode with optical frequency of \( \omega_5 \) through the multistep of interband transitions represented in Figs. 2(a) and 2(b). The optimal lengths of the modulation regions providing maximum frequency conversion efficiency are obtained as \( l_{p_1-\rho_2} = 7.3 \, \mu m, \rho_2-p_3 = 6.85 \, \mu m, l_{p_3-p_4} = 6.4 \, \mu m, \) and \( l_{p_4-p_5} = 6.05 \, \mu m \) from the numerical calculation data.

In the case of a single intraband transition, two transitions to higher frequency mode, \( p_1 \to p_5 \), and lower frequency mode, \( p_1 \to \rho_5 \), occur simultaneously, as shown in Fig. 3(a), which is the origin of inefficiency in frequency conversion. In Fig. 3(b), the length of the optimal modulation region is \( l_{p_1-\rho_2} = 4.55 \, \mu m \). As shown in Fig. 3(b), the optical beating induced by two coherently superposed optical modes \( p_3 \) and \( \rho_5 \) is observed after the modulation region and the optical power exchange along the \( z \) axis is presented.

Comparing interband and intraband photonic transitions, we can see that the frequency conversion efficiency of the proposed multistep interband transitions is above 90%, which is two-times superior to that of the single intraband transitions less than 50%. Cascaded \( n \)-step interband transitions would give low conversion efficiency less than \((50\%)^n\). The proposed multistep configuration with large dynamic range of frequency conversion can provide the physical mechanism necessary for advanced photonic devices, such as photonic diodes, modulators, and transistors.

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References